

(e) Folded form (CFLOBDD) (f) Path corresponding to the

assignment  $[x_0 \mapsto T, x_1 \mapsto T]$ 

Figure 1:

(d) Fully expanded form

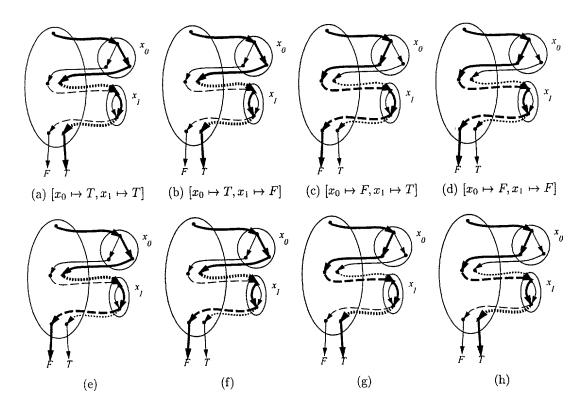
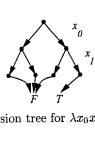
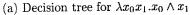


Figure 2:



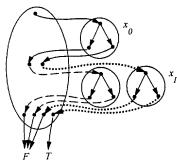




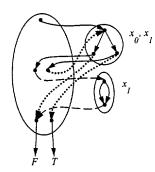
(b) Folded form (OBDD)



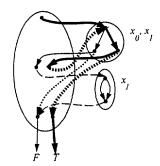
(c) Path corresponding to the assignment  $[x_0 \mapsto T, x_1 \mapsto T]$ 



(d) Fully expanded form

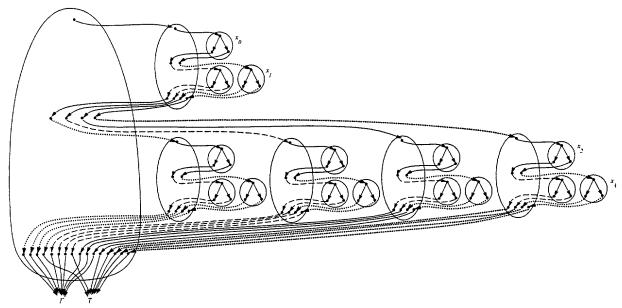


(e) Folded form (CFLOBDD)

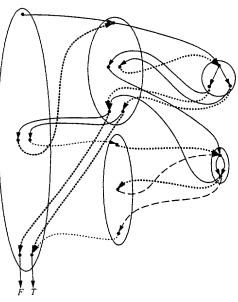


(f) Path corresponding to the assignment  $[x_0 \mapsto T, x_1 \mapsto T]$ 

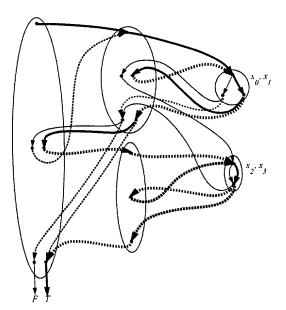
Figure 3:



(a) Fully expanded form for  $\lambda x_0 x_1 x_2 x_3. (x_0 \wedge x_1) \vee (x_2 \wedge x_3)$ 



(b) Folded form (CFLOBDD)



(c) Path corresponding to the assignment  $[x_0 \mapsto T, x_1 \mapsto T, x_2 \mapsto T, x_3 \mapsto T]$ 

Figure 4:

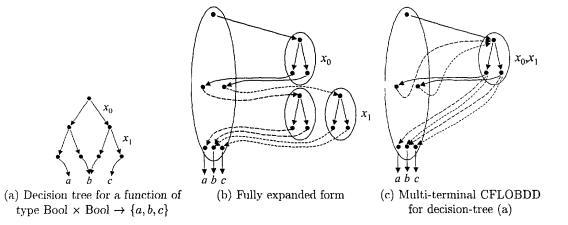
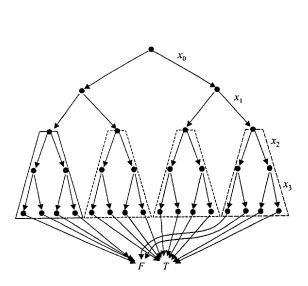
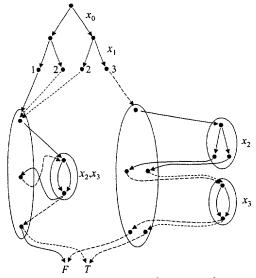


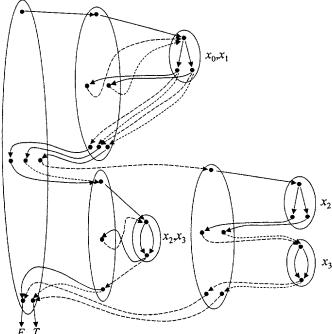
Figure 5:



(a) Decision tree for the function  $\lambda x_0 x_1 x_2 x_3 . (x_0 \oplus x_1) \vee (x_0 \wedge x_1 \wedge x_2)$ .



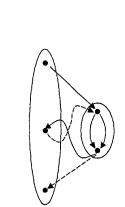
(b) Hybrid of decision tree for  $x_0$  and  $x_1$ , and CFLOBDDs for  $x_2$  and  $x_3$ , for the function  $\lambda x_0 x_1 x_2 x_3.(x_0 \oplus x_1) \vee (x_0 \wedge x_1 \wedge x_2)$ . The solid, dotted, and dashed edges from the four vertices labeled 1, 2, 2, and 3, respectively, correspond to the solid, dotted, and dashed trapezoids in (a).

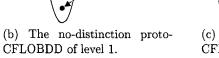


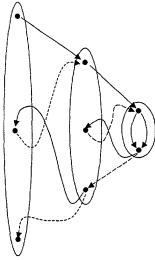
(c) CFLOBDD for the function  $\lambda x_0 x_1 x_2 x_3 . (x_0 \oplus x_1) \vee (x_0 \wedge x_1 \wedge x_2)$ . (For clarity, some of the level-0 groupings have been duplicated.) The dotted and dashed edges in the lower half of the diagram correspond to the analogous edges in (b).

Figure 6:

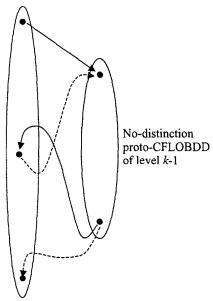
(a) The no-distinction proto-CFLOBDD of level 0.







(c) The no-distinction proto-CFLOBDD of level 2.



(d) Schematic drawing showing how the no-distinction proto-CFLOBDD of level k is constructed from the no-distinction proto-CFLOBDD of level k-1

Figure 7:

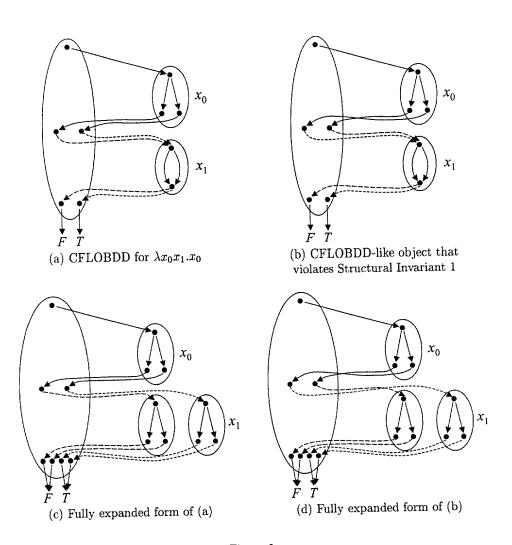


Figure 8:

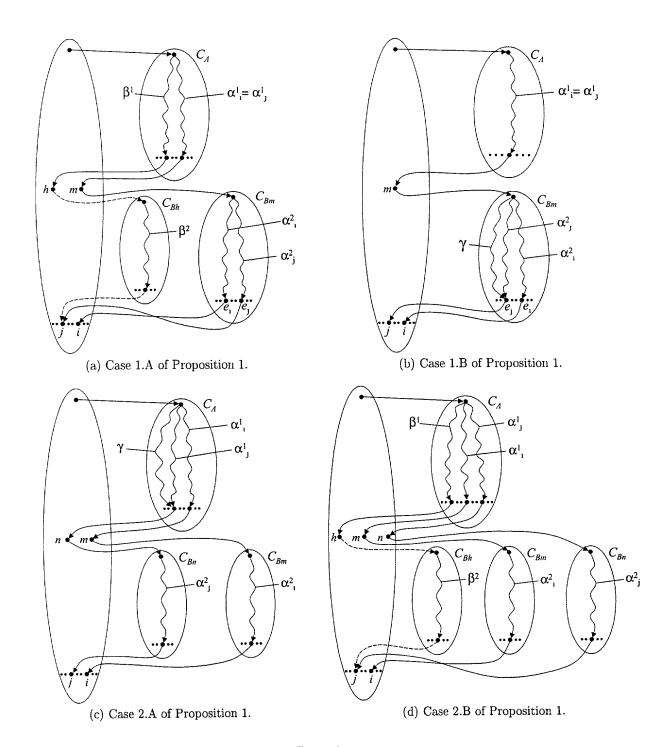


Figure 9:

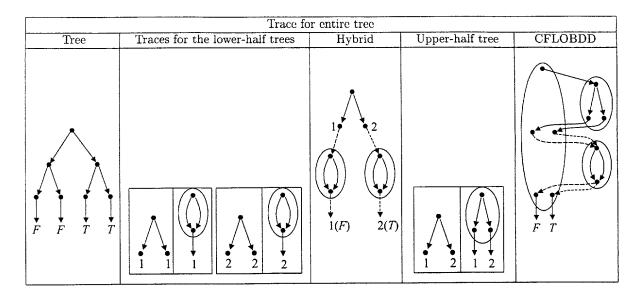


Figure 10: The *Fold* trace generated by the application of Algorithm 1 to the decision tree shown in Figure 1(a) to create the CFLOBDD shown in Figure 1(e).

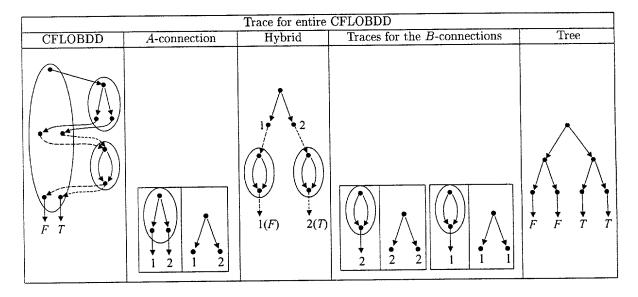


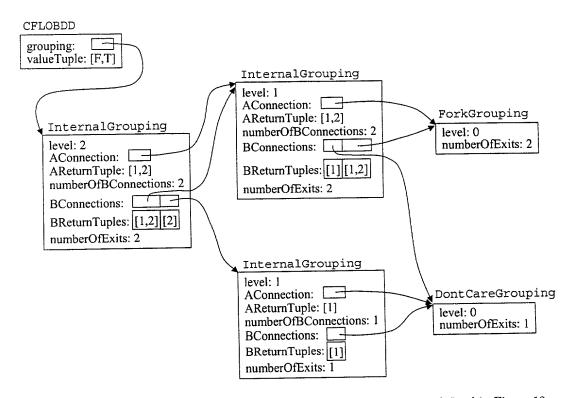
Figure 11: The *Unfold* trace generated by the application of *Unfold* to the CFLOBDD shown in Figure 1(e) to create the decision tree shown in Figure 1(a).

```
[1]
      abstract class Grouping {
[2]
        level: int
[3]
        numberOfExits: int
[4]
      class InternalGrouping extends Grouping {
[5]
        AConnection: Grouping
[6]
        AReturnTuple: ReturnTuple
[7]
[8]
        numberOfBConnections: int
        BConnections: array[1..numberOfBConnections] of Grouping
[9]
        BReturnTuples: array[1..numberOfBConnections] of ReturnTuple
[10]
[11] }
      class DontCareGrouping extends Grouping {
[12]
[13]
        level = 0
        numberOfExits = 1
[14]
[15]
      class ForkGrouping extends Grouping {
[16]
[17]
        level = 0
        numberOfExits = 2
[18]
[19]
      class CFLOBDD { // Multi-terminal CFLOBDD
[20]
        grouping: Grouping
[21]
        valueTuple: ValueTuple
[22]
[23]
```

Figure 12:

```
a set consisting of the elements x_1, \ldots, x_n
\{x_1,\ldots,x_n\}
                                 a tuple consisting of the elements x_1, \ldots, x_n, in order
[x_1,\ldots,x_n]
                                 a map in which x_1 maps to y_1, \ldots, x_n maps to y_n
\{[x_1,y_1],\ldots,[x_n,y_n]\}
                                 the empty set
{}
                                 the empty tuple
the tuple formed by appending t to the right end of tuple T
T||t
                                 the pair [U, v], where U||v = T
SplitOnLast(T)
                                 the number of elements in set S and tuple T, respectively
|S|, |T|
                                 the i^{th} element of tuple T
T(i)
                                 a tuple consisting of the elements i, i+1, i+2, \ldots, j, in order
[i..j], where i, j are integers
                                 set former
\{exp: iterator\}
                                 tuple former
[exp:iterator]
```

Figure 13:



The CFLOBDD from Figure 4(b) depicted as an instance of the class CFLOBDD defined in Figure 12.

Figure 14:

```
[1]
      CFLOBDD ConstantCFLOBDD(int k, value v) {
[2]
       return RepresentativeCFLOBDD(NoDistinctionProtoCFLOBDD(k),[v])
[3]
      CFLOBDD FalseCFLOBDD(int k) {
[4]
[5]
       return ConstantCFLOBDD(k,F)
[6]
      CFLOBDD TrueCFLOBDD(int k) {
[7]
       return ConstantCFLOBDD(k,T)
[8]
[9]
[10] InternalGrouping NoDistinctionProtoCFLOBDD(int k) \{
        if (k == 0) return RepresentativeDontCareGrouping
[11]
[12]
        InternalGrouping g = new InternalGrouping(k)
        g.AConnection = NoDistinctionProtoCFLOBDD(k-1)
[13]
[14]
        g.AReturnTuple = [1]
        g.numberOfBConnections = 1
[15]
        g.BConnections[1] = g.AConnection
[16]
[17]
        g.BReturnTuples[1] = [1]
        g.numberOfExits = 1
[18]
        return RepresentativeGrouping(g)
[19]
[20] }
```

Figure 15:

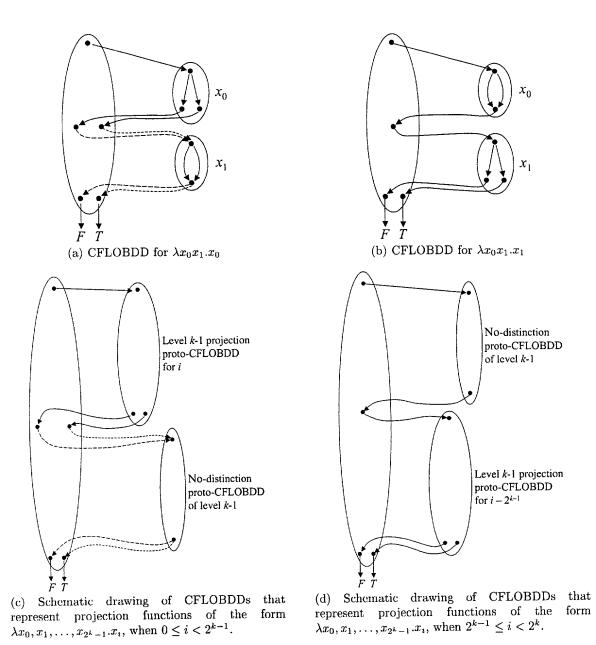
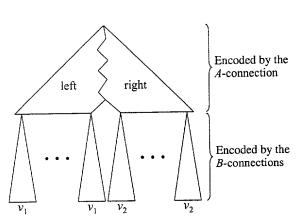


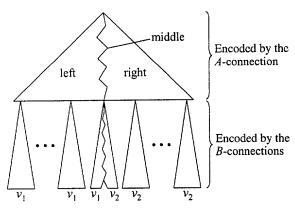
Figure 16:

```
[1]
     CFLOBDD ProjectionCFLOBDD(int k, int i) {
[2]
        assert(0 <= i < 2**k)
        return RepresentativeCFLOBDD(ProjectionProtoCFLOBDD(k,i),[F,T])
[3]
[4]
     }
      Grouping ProjectionProtoCFLOBDD(int k, int i) {
[5]
[6]
        if (k == 0) { // i must also be 0}
[7]
          return RepresentativeForkGrouping
[8]
        else { // Create an appropriate InternalGrouping
[9]
          InternalGrouping g = new InternalGrouping(k)
[10]
          if (i < 2**(k-1)) { // i falls in AConnection range
[11]
            g.AConnection = ProjectionProtoCFLOBDD(k-1,i)
[12]
            g.AReturnTuple = [1,2]
[13]
            g.numBConnections = 2
[14]
            g.BConnection[1] = NoDistinctionProtoCFLOBDD(k-1)
[15]
            g.BReturnTuples[1] = [1]
[16]
            g.BConnection[2] = g.BConnection[1]
[17]
            g.BReturnTuples[2] = [2]
[18]
            g.numExits = 2
[19]
[20]
          else { // i falls in BConnection range
[21]
            g.AConnection = NoDistinctionProtoCFLOBDD(k-1)
[22]
[23]
            g.AReturnTuple = [1]
            g.numBConnections = 1
[24]
            i = i - 2**(k-1)) // Remove high-order bit for recursive call
[25]
            g.BConnection[1] = ProjectionProtoCFLOBDD(k-1,i)
[26]
            g.BReturnTuples[1] = [1,2]
[27]
            g.numExits = 2
[28]
[29]
          return RepresentativeGrouping(g)
[30]
[31]
[32]
```

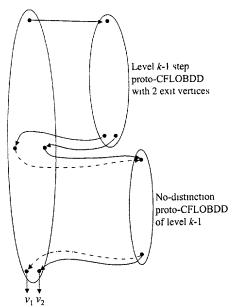
Figure 17:



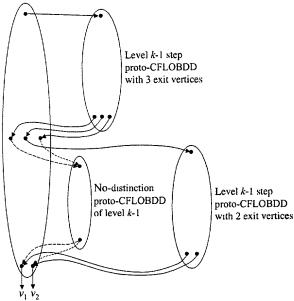
(a) Decision tree for a step function in which the step is made at a value  $i = [x_0x_1 \dots x_{2^k-1}]$  such that  $i \mod 2^{2^{k-1}} = 0$ .



(c) Decision tree for a step function in which the step is made at a value  $i = [x_0x_1 \dots x_{2^k-1}]$  such that  $i \mod 2^{2^{k-1}} \neq 0$ .



(b) Schematic drawing showing the structure of a level-k CFLOBDD for a step function in which the step is made at a value  $i = [x_0x_1 \dots x_{2^k-1}]$  such that  $i \mod 2^{2^{k-1}} = 0$ .



(d) Schematic drawing showing the structure of a level-k CFLOBDD for a step function in which the step is made at a value  $i = [x_0x_1 \dots x_{2^k-1}]$  such that  $i \mod 2^{2^{k-1}} \neq 0$ .

Figure 18:

```
[1]
      CFLOBDD StepCFLOBDD(int k, int i, value v1, value v2) {
        assert(0 <= i <= 2**(2**k))
[2]
[3]
        if (v1 == v2) return RepresentativeCFLOBDD(NoDistinctionProtoCFLOBDD(k),[v1])
[4]
        if (i == 0) return RepresentativeCFLOBDD(NoDistinctionProtoCFLOBDD(k),[v2])
[5]
        if (i == 2**(2**k)) return RepresentativeCFLOBDD(NoDistinctionProtoCFLOBDD(k),[v1])
[6]
        Grouping g = StepProtoCFLOBDD(k, i, 0, 2**(2**k) - i)
[7]
        return RepresentativeCFLOBDD(g,[v1,v2])
[8]
[9]
     Grouping StepProtoCFLOBDD(int k, int left, int middle, int right) {
[10]
        assert(middle == 0 | middle == 1)
[11]
        assert(left + middle + right == 2**(2**k))
[12]
        if (k == 0) { // Base case
[13]
         if (left == 2 || right == 2) return RepresentativeDontCareGrouping
[14]
          else return RepresentativeForkGrouping
[15]
        InternalGrouping g = new InternalGrouping(k)
[16]
[17]
        g.numberOfExits = (left != 0) + (middle != 0) + (right != 0)
[18]
        int P = 2**(2**(k-1))
        int a = left/P // a holds the 2**(k-1) most-significant bits of left
[19]
[20]
        int c = right/P // c holds the 2**(k-1) most-significant bits of right
        int b = (left mod P + right mod P)/P + middle // 0 for Fig.18(a); 1 for Fig.18(c)
[21]
       // Create the AConnection -----
[22]
[23]
        int numberOfAExits = (a != 0) + (b != 0) + (c != 0) // Upto 3 exits
[24]
        g.AConnection = StepProtoCFLOBDD(k-1, a, b, c)
[25]
        g.AReturnTuple = [1..numberOfAExits]
[26]
       // Create the BConnections ------
[27]
       g.numBConnections = numberOfAExits
[28]
        int curConnection = 1
[29]
       if (a != 0) {
[30]
         g.BConnection[curConnection] = NoDistinctionProtoCFLOBDD(k-1)
[31]
          g.BReturnTuples[curConnection] = [1]
[32]
         curConnection = curConnection + 1
[33]
       if (b != 0) {
[34]
[35]
         int aa = left mod P
[36]
         int cc = right mod P
[37]
         int bb = middle
[38]
         g.BConnection[curConnection] = StepProtoCFLOBDD(k-1, aa, bb, cc)
[39]
         ReturnTuple rt
[40]
         if (aa != 0) rt = rt || 1 // Connect to first exit
[41]
         if (bb != 0)
[42]
           if (left != 0) rt = rt || 2
[43]
           else rt = rt || 1
[44]
         if (cc != 0) rt = rt || g.numberOfExits // Connect to last exit
[45]
         g.BReturnTuples[curConnection] = rt
         curConnection = curConnection + 1
[46]
[47]
[48]
       if (c != 0) {
[49]
         g.BConnection[curConnection] = NoDistinctionProtoCFLOBDD(k-1)
[50]
         g.BReturnTuples[curConnection] = [g.numberOfExits] // Connect to last exit
[51]
[52]
       return RepresentativeGrouping(g)
[53] }
```

Figure 19:

```
[1]
     CFLOBDD FlipValueTupleCFLOBDD(CFLOBDD c) {
[2]
        assert(|c.valueTuple| == 2)
[3]
       return RepresentativeCFLOBDD(c.grouping,[c.valueTuple[2],c.valueTuple[1]])
[4]
     CFLOBDD ComplementCFLOBDD(CFLOBDD c) {
[5]
        if (c == FalseCFLOBDD(c.grouping.level)) return TrueCFLOBDD(c.grouping.level)
[6]
        if (c == TrueCFLOBDD(c.grouping.level)) return FalseCFLOBDD(c.grouping.level)
[7]
[8]
       return FlipValueTupleCFLOBDD(c)
[9]
```

Figure 20:

```
[1] CFLOBDD ScalarMultiplyCFLOBDD(CFLOBDD c, Value v) {
[2]    if (v == zero) return ConstantCFLOBDD(c.level,zero)
[3]    return RepresentativeCFLOBDD(c.grouping,[v*c.valueTuple(i) | i ∈ [1..|c.valueTuple]])
[4] }
```

Figure 21:

```
[1]
      Tuple XTuple CollapseClassesLeftmost(Tuple equivClasses) {
[2]
        // Project the tuple equivClasses, preserving left-to-right order,
[3]
        // retaining the leftmost instance of each class
[4]
        Tuple projectedClasses =
[5]
              [ equivClasses(i)
[6]
              : i \in [1..|equivClasses|]
[7]
              | i = min\{j \in [1..|equivClasses|] | equivClasses(j) = equivClasses(i)\}
[8]
              ٦
[9]
        // Create tuple in which classes in equivClasses are renumbered
[10]
        // according to their ordinal position in projectedClasses
[11]
        Map orderOfProjectedClasses =
                \{[x,i] : i \in [1..|projectedClasses|] \mid x = projectedClasses(i)\}
[12]
[13]
        Tuple renumberedClasses = [orderOfProjectedClasses(v) : v \in equivClasses ]
        return [projectedClasses, renumberedClasses]
[14]
[15] }
```

## Figure 22:

```
CFLOBDD BinaryApplyAndReduce(CFLOBDD n1, CFLOBDD n2, Op op) {
[1]
[2]
        assert(n1.grouping.level == n2.grouping.level)
[3]
        // Perform cross product
        Grouping×PairTuple [g,pt] = PairProduct(n1.grouping,n2.grouping)
[4]
        // Create tuple of ''leaf'' values
[5]
        ValueTuple deducedValueTuple =
[6]
                   [ op(n1.valueTuple[i1],n2.valueTuple[i2]) : [i1,i2] \in pt ]
[7]
        // Collapse duplicate leaf values, folding to the left
[8]
        Tuple X Tuple [inducedValueTuple,inducedReductionTuple] =
[9]
[10]
                     CollapseClassesLeftmost(deducedValueTuple)
[11]
        // Perform corresponding reduction on g,
        // folding g's exit vertices w.r.t. inducedReductionTuple
[12]
        Grouping g' = Reduce(g, inducedReductionTuple)
[13]
        return RepresentativeCFLOBDD(g', inducedValueTuple)
[14]
[15] }
```

Figure 23:

```
Grouping × PairTuple PairProduct(Grouping g1, Grouping g2) {
[1]
       if (g1 and g2 are both no-distinction proto-CFLOBDDs) return [ g1, [[1,1]] ]
[2]
       if (g1 is a no-distinction proto-CFLOBDD)
[3]
         return [ g2, [[1,k] : k ∈ [1..g2.numberOfExits]] ]
[4]
       if (g2 is a no-distinction proto-CFLOBDD)
[5]
         return [ g1, [[k,1] : k ∈ [1..g1.numberOfExits]] ]
[6]
       if (g1 and g2 are both fork groupings) return [ g1, [[1,1],[2,2]] ]
[7]
       // Pair the A-connections -----
[8]
       Grouping × PairTuple [gA,ptA] = PairProduct(g1.AConnection,
[9]
                                                 g2.AConnection)
[10]
       InternalGrouping g = new InternalGrouping(g1.level)
[11]
       g.AConnection = gA
[12]
       g.AReturnTuple = [1..|ptA|] // Represents the middle vertices
[13]
[14]
       g.numberOfBConnections = |ptA|
        // Pair the B-connections, but only for pairs in ptA -----
[15]
        Tuple ptAns = [] // Descriptor of pairings of exit vertices
[16]
        for (j = 1; j \le |ptA|; j++)  // Create a B-connection for each middle vertex
[17]
          Grouping × PairTuple [gB,ptB] = PairProduct(g1.BConnections[ptA(j)(1)],
Γ187
                                                   g2.BConnections[ptA(j)(2)])
[19]
          g.BConnections[j] = gB
[20]
          // Now create g.BReturnTuples[j], and augment ptAns as necessary
[21]
          g.BReturnTuples[j] = []
[22]
          for (i = 1; i <= |ptB|; i++) {
[23]
            c1 = g1.BReturnTuples[ptA(j)(1)](ptB(i)(1)) // an exit vertex of g1
[24]
            c2 = g2.BReturnTuples[ptA(j)(2)](ptB(i)(2)) // an exit vertex of g2
[25]
            if([c1,c2] \in ptAns) { // Not a new exit vertex of g
[26]
              index = the k such that ptAns(k) == [c1,c2]
[27]
              g.BReturnTuples[j] = g.BReturnTuples[j] || index
[28]
[29]
            else { // Identified a new exit vertex of g
[30]
              g.numberOfExits = g.numberOfExits + 1
[31]
              g.BReturnTuples[j] = g.BReturnTuples[j] || g.numberOfExits
[32]
              ptAns = ptAns || [c1,c2]
[33]
[34]
[35]
          }
[36]
        }
[37]
        return [RepresentativeGrouping(g), ptAns]
[38] }
```

Figure 24:

```
// Insert h, ReturnTuple as next B-connection of g, if they are a new combination;
[1]
      // otherwise, return the index of the existing occurrence of h, ReturnTuple
[2]
      int InsertBConnection(InternalGrouping g, Grouping h, ReturnTuple returnTuple) {
[3]
        for (i = 1; i <= g.numberOfBConnections; i++) {</pre>
[4]
          if (g.BConnections[i] == h && g.BReturnTuples[i] == returnTuple) return i
[5]
[6]
        // Not found -- insert h, ReturnTuple as next B-connection of g
[7]
        g.numberOfBConnections = g.numberOfBConnections + 1
[8]
        g.BConnections[g.numberOfBConnections] = h
[9]
[10]
        g.BReturnTuples[g.numberOfBConnections] = returnTuple
[11]
        return g.numberOfBConnections
[12] }
[13]
      Grouping Reduce(Grouping g, ReductionTuple reductionTuple) {
        // Test whether any reduction actually needs to be carried out
[14]
        if (reductionTuple == [1..|reductionTuple|]) return g
[15]
[16]
        // If only one exit vertex, then collapse to no-distinction proto-CFLOBDD
        if (|\{x : x \in reductionTuple \}| == 1) return NoDistinctionProtoCFLOBDD(g.level)
[17]
        InternalGrouping g' = new InternalGrouping(g.level)
[18]
[19]
        g'.numberOfExits = |{x : x ∈ reductionTuple }|
[20]
        // Reduce each B-connection of g w.r.t. reductionTuple, while gathering
[21]
        // information in reductionTupleA about how to reduce the A-connection of g
[22]
        Tuple reductionTupleA = []
[23]
        for (i = 1; i <= g.numberOfBConnections; i++) {</pre>
          \label{eq:turnClasses} \mbox{Tuple deducedReturnClasses = [ reductionTuple(v) : v \in g.BReturnTuples[i] ]}
[24]
[25]
          Tuple X Tuple [inducedReturnTuple, inducedReductionTuple] =
[26]
                       CollapseClassesLeftmost(deducedReturnClasses)
[27]
          // Perform reduction on g.BConnections[i], w.r.t. inducedReductionTuple
[28]
          Grouping h = Reduce(g.BConnection[i], inducedReductionTuple)
[29]
          // Insert h,inducedReturnTuple as next B-connection, but only if new
[30]
          int position = InsertBConnection(g', h, inducedReturnTuple)
[31]
          // Build up the tuple that indicates how to reduce the A-connection
[32]
          reductionTupleA = reductionTupleA || position
[33]
        }
[34]
        // Reduce the A-connection w.r.t. reductionTupleA
        Tuple × Tuple [inducedReturnTuple, inducedReductionTuple] =
[35]
[36]
                     CollapseClassesLeftmost(reductionTupleA)
        // Perform reduction on g.AConnection, w.r.t. inducedReductionTuple
[37]
[38]
        Grouping h' = Reduce(g.AConnection,inducedReductionTuple)
[39]
        g'.AConnection = h'
[40]
        g'.AReturnTuple = inducedReturnTuple
        return RepresentativeGrouping(g')
[41]
[42] }
```

Figure 25:

```
CFLOBDD TernaryApplyAndReduce(CFLOBDD n1, CFLOBDD n2, CFLOBDD n3, Op op) {
[1]
        assert(n1.grouping.level == n2.grouping.level && n2.grouping.level == n3.grouping.level)
[2]
        // Perform triple cross product
[3]
        Grouping × Triple Tuple [g,tt] = Triple Product(n1.grouping,n2.grouping,n3.grouping)
[4]
        // Create tuple of ''leaf'' values
[5]
        ValueTuple deducedValueTuple =
[6]
                   [ op(n1.valueTuple[i1],n2.valueTuple[i2],n3.valueTuple[i3]) : [i1,i2,i3] \in tt ]
[7]
        // Collapse duplicate leaf values, folding to the left
[8]
        Tuple X Tuple [inducedValueTuple, inducedReductionTuple] =
[9]
                    CollapseClassesLeftmost(deducedValueTuple)
[10]
[11]
        // Perform corresponding reduction on g,
        // folding g's exit vertices w.r.t. inducedReductionTuple
[12]
        Grouping g' = Reduce(g, inducedReductionTuple)
[13]
        return RepresentativeCFLOBDD(g', inducedValueTuple)
[14]
[15] }
```

Figure 26:

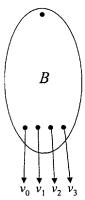
```
Grouping x TripleTuple TripleProduct(Grouping g1, Grouping g2, Grouping g3) {
[1]
        if (g1, g2, and g3 are all no-distinction proto-CFLOBDDs) return [ g1, [[1,1,1]] ]
[2]
        if (g1 and g2 are no-distinction proto-CFLOBDDs)
[3]
         return [g3, [[1,1,k] : k \in [1..g3.numberOfExits]]
[4]
[5]
        if (g1 and g3 are no-distinction proto-CFLOBDDs)
         return [ g2, [[1,k,1] : k \in [1..g2.numberOfExits]]
[6]
        if (g2 and g3 are no-distinction proto-CFLOBDDs)
[7]
         return [ g1, [[k,1,1] : k \in [1..g1.number0fExits]] ]
[8]
[9]
        if (g1 is a no-distinction proto-CFLOBDD) {
          Grouping × PairTuple [g,pt] = PairProduct(g2,g3)
[10]
         return [g, [[1,j,k]: [j,k] \in pt]]
[11]
[12]
        if (g2 is a no-distinction proto-CFLOBDD) {
[13]
          Grouping×PairTuple [g,pt] = PairProduct(g1,g3)
[14]
          return [g, [[j,1,k]: [j,k] \in pt]]
[15]
[16]
        if (g3 is a no-distinction proto-CFLOBDD) {
[17]
          Grouping×PairTuple [g,pt] = PairProduct(g1,g2)
[18]
          return [g, [[j,k,1]: [j,k] \in pt]]
[19]
[20]
        if (g1, g2, and g3 are all fork groupings) return [ g1, [[1,1,1],[2,2,2]] ]
[21]
        // Combine the A-connections -----
[22]
        Grouping × TripleTuple [gA,ttA] = TripleProduct(g1.AConnection,
[23]
                                                       g2.AConnection,
[24]
                                                       g3.AConnection)
[25]
        InternalGrouping g = new InternalGrouping(g1.level)
[26]
[27]
        g.AConnection = gA
        g.AReturnTuple = [1..|ttA|] // Represents the middle vertices
[28]
        g.numberOfBConnections = |ttA|
[29]
        // Combine the B-connections, but only for triples in ttA -----
[30]
        Tuple ttAns = [] // Descriptor of triples of exit vertices
[31]
        for (j = 1; j \le |ttA|; j++) \{ // Create a B-connection for each middle vertex \}
[32]
          Grouping x Triple Tuple [gB,ttB] = Triple Product(g1.BConnections[ttA(j)(1)],
[33]
                                                         g2.BConnections[ttA(j)(2)],
[34]
                                                         g3.BConnections[ttA(j)(3)])
[35]
[36]
          g.BConnections[j] = gB
          // Now create g.BReturnTuples[j], and augment ttAns as necessary
[37]
[38]
          g.BReturnTuples[j] = []
          for (i = 1; i <= |ttB|; i++) {
[39]
             c1 = g1.BReturnTuples[ttA(j)(1)](ttB(i)(1)) // an exit vertex of g1
[40]
             c2 = g2.BReturnTuples[ttA(j)(2)](ttB(i)(2)) // an exit vertex of g2
[41]
             c3 = g3.BReturnTuples[ttA(j)(3)](ttB(i)(3)) // an exit vertex of g3
[42]
             if([c1,c2,c3] \in ttAns) \{ // Not a new exit vertex of g
[43]
[44]
               index = the k such that ttAns(k) == [c1, c2, c3]
               g.BReturnTuples[j] = g.BReturnTuples[j] || index
[45]
[46]
[47]
             else { // Identified a new exit vertex of g
               g.numberOfExits = g.numberOfExits + 1
[48]
[49]
               g.BReturnTuples[j] = g.BReturnTuples[j] || g.numberOfExits
[50]
               ttAns = ttAns \mid | [c1,c2,c3]
[51]
[52]
          }
[53]
[54]
        return [RepresentativeGrouping(g), ttAns]
[55] }
```

Touth Toble	Defining Expression	Definition Using ITE
Truth Table	Demning Expression	Demicion Using 11D
$egin{array}{cccc} F & T & T & F & F & F & F & F & F & F &$	$\lambda a, b.F$	$\lambda a, b.F$
$egin{array}{cccc} & & & b & & & & & & & & & & & & & & & $	$\lambda a, b.a \wedge b$	$\lambda a, b.  ext{ITE}(a,b,F)$
$egin{array}{cccc} & & & & & & b & & & & & & & & & & & & $	$\lambda a, b.a \wedge \neg b$	$\lambda a, b.  ext{ITE}(a, \neg b, F)$
$egin{array}{cccc} & & & & b & & & & & & & & & & & & & & $	$\lambda a, b.a$	$\lambda a, b.a$
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	$\lambda a, b, \neg a \wedge b$	$\lambda a, b.  ext{ITE}(a, F, b)$
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	$\lambda a, b.b$	$\lambda a, b.b$
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	$\lambda a, b.a \oplus b$	$\lambda a, b. \text{ITE}(a, \neg b, b)$
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	$\lambda a, b.a \lor b$	$\lambda a, b.  ext{ITE}(a, T, b)$
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	$\lambda a, b, \neg(a \lor b)$	$\lambda a, b. \text{ITE}(a, F, \neg b)$
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	$\lambda a, b. \neg (a \oplus b)$	$\lambda a, b. \text{ITE}(a, b, \neg b)$
$\begin{array}{c c} & & b \\ F & T \\ \hline a & F & T & F \\ T & F \end{array}$	$\lambda a, b. \neg b$	$\lambda a, b.  ext{ITE}(b, F, T)$
$\begin{array}{c c} & & b \\ F & T \\ \hline a & F & T \\ \hline T & T \\ \end{array}$	$\lambda a, b.a \lor \neg b$	$\lambda a, b.  ext{ITE}(a, T, \neg b)$
$\begin{bmatrix} & & & b \\ F & T \\ a & F & T & T \\ F & F \end{bmatrix}$	$\lambda a, b. \neg a$	$\lambda a, b.  ext{ITE}(a, F, T)$
$\begin{bmatrix} & & b \\ F & T \\ a & F & T \\ T & T \\ F & T \end{bmatrix}$	$\lambda a, b. \neg a \lor b$	$\lambda a, b.  ext{ITE}(a, b, T)$
$\begin{bmatrix} & & & b \\ F & T \\ a & F & T & T \\ T & F \end{bmatrix}$	$\lambda a, b, \neg (a \wedge b)$	$\lambda a, b. \text{ITE}(a, \neg b, T)$
$\begin{bmatrix} & & b \\ F & T \\ a & F & T \\ T & T \end{bmatrix}$	$\lambda a, b.T$	$\lambda a, b.T$

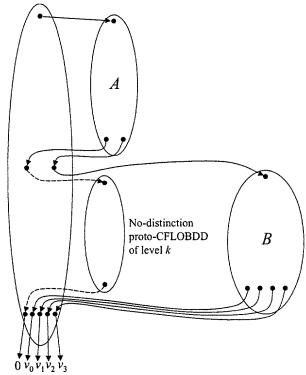
Figure 28:



(a) Level-k CFLOBDD for an array A whose elements are drawn from  $\{0,1\}$ . (Schematic drawing only—details of lower-level groupings are not shown.)

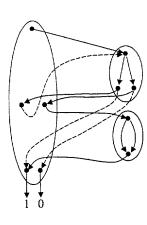


(b) Level-k CFLOBDD for an array B whose elements are drawn from  $\{v_0, v_1, v_2, v_3\}$ . (Schematic drawing only—details of lower-level groupings are not shown.)



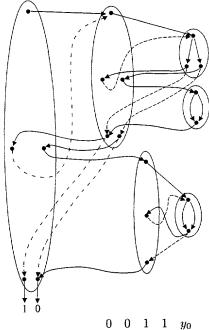
(c) Level k+1 CFLOBDD for array  $A\otimes B$ . (Schematic drawing only—details of lower-level groupings are not shown.)

Figure 29:



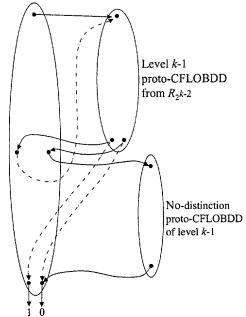
$$R_1 = \begin{array}{cc} & 0 & 1 & y_0 \\ 0 & 1 & 1 & 0 \\ 1 & x_0 & 1 & 1 \end{array}$$

(a) Level-1 CFLOBDD for the 2  $\times$  2 Reed-Muller transform matrix  $R_1$ , under the interleaved variable ordering.



			0	0	1	1	$y_0$
			0	1	0	1	$y_1$
	0	0	1	0	0	0	
$R_2 =$	0	1	1	1	0	0	
	1	0	1	0	1	0	
	1	1	1	1	1	1	
	$x_0$	$x_1$					

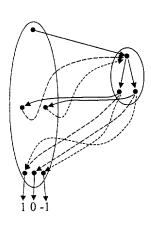
(b) Level-2 CFLOBDD for the  $4 \times 4$  Reed-Muller transform matrix  $R_2$ , under the interleaved variable ordering.



(c) Schematic drawing showing how, under the interleaved variable ordering, the level-k CFLOBDD for the  $2^{2^{k-1}} \times 2^{2^{k-1}}$  Reed-Muller transform matrix  $R_{2^{k-1}} = R_{2^{k-2}} \otimes R_{2^{k-2}}$  is constructed from two level k-1 proto-CFLOBDDs.

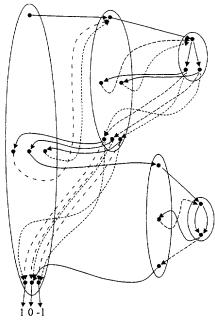
```
[1]
      CFLOBDD ReedMullerCFLOBDD(int i) {
        return RepresentativeCFLOBDD(ReedMullerProtoCFLOBDD(i),[1,0])
[2]
[3]
      InternalGrouping ReedMullerProtoCFLOBDD(int i) {
[4]
[5]
        InternalGrouping g = new InternalGrouping(i)
[6]
        if (i == 1) {
[7]
          g.AConnection = RepresentativeForkGrouping
[8]
          g.AReturnTuple = [1,2]
[9]
          g.numberOfBConnections = 2
          g.BConnections[1] = RepresentativeForkGrouping
[10]
          g.BReturnTuples[1] = [1,2]
[11]
          g.BConnections[2] = RepresentativeDontCareGrouping
[12]
          g.BReturnTuples[2] = [1]
[13]
[14]
[15]
        else {
          g.AConnection = ReedMullerProtoCFLOBDD(i-1)
[16]
          g.AReturnTuple = [1,2]
[17]
          g.numberOfBConnections = 2
[18]
          g.BConnections[1] = g.AConnection
[19]
          g.BReturnTuples[1] = [1,2]
[20]
          g.BConnections[2] = NoDistinctionProtoCFLOBDD(i-1)
[21]
          g.BReturnTuples[2] = [2]
[22]
[23]
[24]
        g.numberOfExits = 2
[25]
        return RepresentativeGrouping(g)
[26]
```

Figure 31:



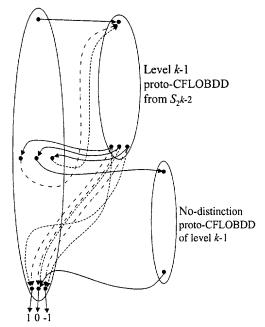
$$S_1 = \begin{array}{ccc} 0 & 1 & y_0 \\ 1 & \hline -1 & 1 \\ x_0 \end{array}$$

(a) Level-1 CFLOBDD for the  $2 \times 2$  inverse Reed-Muller transform matrix  $S_1$ , under the interleaved variable ordering.



			0	0	1	1	$y_0$
			0	1	0	1	$y_1$
	0	0	1	0	0	0	
$S_2 =$	0	1	-1	1	0	0	
	1	0	-1	0	1	0	
	1	1	1	-1	-1	1	
	$x_0$	$x_1$					

(b) Level-2 CFLOBDD for the  $4 \times 4$  inverse Reed-Muller transform matrix  $S_2$ , under the interleaved variable ordering.

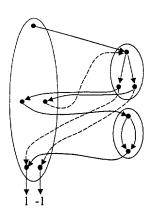


(c) Schematic drawing showing how, under the interleaved variable ordering, the level-k CFLOBDD for the  $2^{2^{k-1}} \times 2^{2^{k-1}}$  inverse Reed-Muller transform matrix  $S_{2^{k-1}} = S_{2^{k-2}} \otimes S_{2^{k-2}}$  is constructed from two level k-1 proto-CFLOBDDs.

Figure 32:

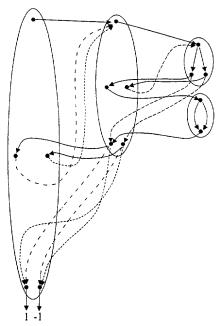
```
[1]
     CFLOBDD InverseReedMullerCFLOBDD(int i) {
        return RepresentativeCFLOBDD(InverseReedMullerProtoCFLOBDD(i),[1,0,-1])
[2]
[3]
      }
[4]
      InternalGrouping InverseReedMullerProtoCFLOBDD(int i) {
        InternalGrouping g = new InternalGrouping(i)
[5]
[6]
        if (i == 1) {
[7]
          g.AConnection = RepresentativeForkGrouping
[8]
          g.AReturnTuple = [1,2]
[9]
          g.numberOfBConnections = 2
[10]
          g.BConnections[1] = RepresentativeForkGrouping
          g.BReturnTuples[1] = [1,2]
[11]
          g.BConnections[2] = RepresentativeForkGrouping
[12]
[13]
          g.BReturnTuples[2] = [3,1]
[14]
[15]
        else {
          g.AConnection = InverseReedMullerProtoCFLOBDD(i-1)
[16]
[17]
          g.AReturnTuple = [1,2,3]
          g.numberOfBConnections = 3
[18]
[19]
          g.BConnections[1] = g.AConnection
          g.BReturnTuples[1] = [1,2,3]
[20]
          g.BConnections[2] = NoDistinctionProtoCFLOBDD(i-1)
[21]
[22]
          g.BReturnTuples[2] = [2]
[23]
          g.BConnections[3] = g.AConnection
[24]
          g.BReturnTuples[3] = [3,2,1]
[25]
[26]
        g.numberOfExits = 3
[27]
        return RepresentativeGrouping(g)
[28] }
```

Figure 33:



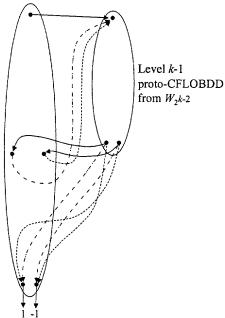
$$W_1 = \begin{array}{ccc} & 0 & 1 \\ 0 & \hline 1 & 1 \\ x_0 & \hline & 1 & -1 \end{array} \\ y_0$$

(a) Level-1 CFLOBDD for the  $2\times 2$  Walsh transform matrix  $W_1$ , under the interleaved variable ordering.



			0	0	1	1	$y_0$
			0	1	0	1	$y_1$
	0	0	1	1	1	1	
$W_2 =$	0	1	1	-1	1	-1	
	1	0	1	1	-1	-1	
	1	1	1	-1	-1	1	
	$x_0$	$x_i$					•

(b) Level-2 CFLOBDD for the  $4 \times 4$  Walsh transform matrix  $W_2$ , under the interleaved variable ordering.

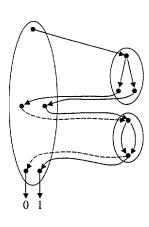


(c) Schematic drawing showing how, under the interleaved variable ordering, the level-k CFLOBDD for the  $2^{2^{k-1}} \times 2^{2^{k-1}}$  Walsh transform matrix  $W_{2^{k-1}} = W_{2^{k-2}} \otimes W_{2^{k-2}}$  is constructed from a level k-1 proto-CFLOBDD.

Figure 34:

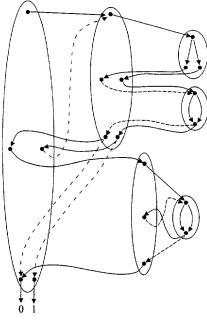
```
[1]
      CFLOBDD WalshCFLOBDD(int i) {
[2]
        return RepresentativeCFLOBDD(WalshProtoCFLOBDD(i),[1,-1])
[3]
[4]
      InternalGrouping WalshProtoCFLOBDD(int i) {
[5]
        InternalGrouping g = new InternalGrouping(i)
[6]
        if (i == 1) {
[7]
          g.AConnection = RepresentativeForkGrouping
[8]
          g.AReturnTuple = [1,2]
[9]
          g.numberOfBConnections = 2
[10]
          g.BConnections[1] = RepresentativeDontCareGrouping
[11]
          g.BReturnTuples[1] = [1]
[12]
          g.BConnections[2] = RepresentativeForkGrouping
[13]
          g.BReturnTuples[2] = [1,2]
[14]
[15]
        else {
[16]
          g.AConnection = WalshProtoCFLOBDD(i-1)
[17]
          g.AReturnTuple = [1,2]
[18]
          g.numberOfBConnections = 2
[19]
          g.BConnections[1] = g.AConnection
[20]
          g.BReturnTuples[1] = [1,2]
[21]
          g.BConnections[2] = g.AConnection
[22]
          g.BReturnTuples[2] = [2,1]
[23]
        g.numberOfExits = 2
[24]
[25]
        return RepresentativeGrouping(g)
[26]
```

Figure 35:



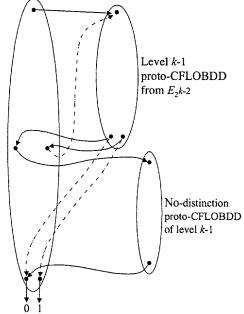
$$E_1 = \begin{array}{cc} & 0 & 1 \\ 0 & 1 & 0 \\ 1 & x_0 & 1 \end{array} y_0$$

(a) Level-1 CFLOBDD for the  $2 \times 2$  matrix  $E_1$ , under the interleaved variable ordering.



			0	0	1	1	$y_0$
			0	1	0	1	$y_1$
	0	0	0	0	0	0	
$E_2 =$	0	1	0	0	0	0	
	1	0	0	0	0	0	
	1	1	1	1	1	1	
	$x_0$	$x_1$					

(b) Level-2 CFLOBDD for the  $4 \times 4$  matrix  $E_2$ , under the interleaved variable ordering.

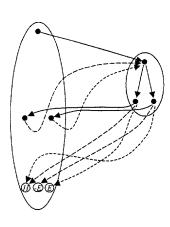


(c) Schematic drawing showing how, under the interleaved variable ordering, the level-k CFLOBDD for the  $2^{2^{k-1}} \times 2^{2^{k-1}}$  matrix  $E_{2^{k-1}} = E_{2^{k-2}} \otimes E_{2^{k-2}}$  is constructed from two level k-1 proto-CFLOBDDs.

Figure 36:

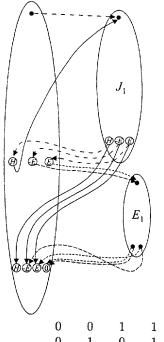
```
[1]
      CFLOBDD ECFLOBDD(int i) {
[2]
        return RepresentativeCFLOBDD(EProtoCFLOBDD(i),[0,1])
[3]
[4]
      InternalGrouping EProtoCFLOBDD(int i) {
[5]
        InternalGrouping g = new InternalGrouping(i)
[6]
        if (i == 1) {
[7]
          g.AConnection = RepresentativeForkGrouping
[8]
          g.AReturnTuple = [1,2]
[9]
          g.numberOfBConnections = 2
[10]
          g.BConnections[1] = RepresentativeDontCareGrouping
[11]
          g.BReturnTuples[1] = [1]
[12]
          g.BConnections[2] = RepresentativeDontCareGrouping
[13]
          g.BReturnTuples[2] = [2]
[14]
[15]
       else {
[16]
          g.AConnection = EProtoCFLOBDD(i-1)
[17]
          g.AReturnTuple = [1,2]
[18]
          g.numberOfBConnections = 2
[19]
          g.BConnections[1] = NoDistinctionProtoCFLOBDD(i-1)
[20]
          g.BReturnTuples[1] = [1]
[21]
          g.BConnections[2] = g.AConnection
[22]
          g.BReturnTuples[2] = [1,2]
[23]
[24]
       g.numberOfExits = 2
[25]
       return RepresentativeGrouping(g)
[26] }
```

Figure 37:



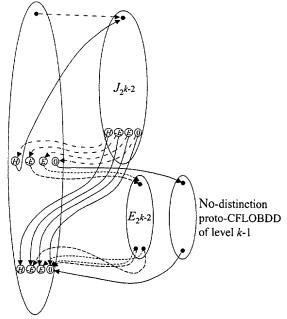
$$J_1 = \begin{array}{ccc} 0 & 1 & y_0 \\ 1 & H & -E \\ E & H \end{array}$$

(a) The level-1 proto-CFLOBDD  $J_1$ , and the 2  $\times$  2 matrix that it represents under the interleaved variable ordering.



			0	$0 \\ 1$	1 0	1 1	$y_0$ $y_1$
	0	0	$\overline{H}$	-E	0	0	
$J_2 =$	0	1	$\mid E \mid$	H	-E	-E	
	1	0	0	0	H	-E	
	1	1	E	E	E	H	
	$x_0$	$x_1$					•

(b) The level-2 proto-CFLOBDD  $J_2$ , and the 4 × 4 matrix that it represents under the interleaved variable ordering.

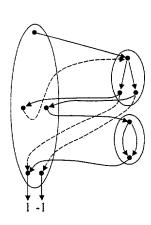


(c) Schematic drawing showing how the level-k proto-CFLOBDD  $J_{2^{k-1}}$ , for  $k \geq 3$ , is constructed from three level k-1 proto-CFLOBDDs.

Figure 38:

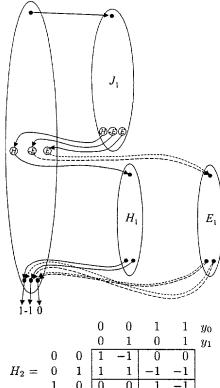
```
[1]
      InternalGrouping JProtoCFLOBDD(int i) {
[2]
        InternalGrouping g = new InternalGrouping(i)
[3]
        if (i == 1) {
[4]
          g.AConnection = RepresentativeForkGrouping
[5]
          g.AReturnTuple = [1,2]
[6]
          g.numberOfBConnections = 2
[7]
          g.BConnections[1] = RepresentativeForkGrouping
[8]
          g.BReturnTuples[1] = [1,2]
[9]
          g.BConnections[2] = RepresentativeForkGrouping
[10]
          g.BReturnTuples[2] = [3,1]
[11]
          g.numberOfExits = 3
[12]
[13]
        else if (i == 2) {
[14]
          g.AConnection = JProtoCFLOBDD(1)
[15]
          g.AReturnTuple = [1,2,3]
[16]
          g.numberOfBConnections = 3
[17]
          g.BConnections[1] = g.AConnection
[18]
          g.BReturnTuples[1] = [1,2,3]
[19]
          g.BConnections[2] = EProtoCFLOBDD(1)
[20]
          g.BReturnTuples[2] = [4,2]
[21]
          g.BConnections[3] = g.BConnections[2]
[22]
          g.BReturnTuples[3] = [4,3]
[23]
          g.numberOfExits = 4
[24]
[25]
        else {
[26]
          g.AConnection = JProtoCFLOBDD(i-1)
[27]
          g.AReturnTuple = [1,2,3,4]
[28]
          g.numberOfBConnections = 4
          g.BConnections[1] = g.AConnection
[29]
[30]
          g.BReturnTuples[1] = [1,2,3,4]
[31]
          g.BConnections[2] = EProtoCFLOBDD(i-1)
[32]
          g.BReturnTuples[2] = [4,2]
[33]
          g.BConnections[3] = g.BConnections[2]
[34]
          g.BReturnTuples[3] = [4,3]
[35]
          g.BConnections[4] = NoDistinctionProtoCFLOBDD(i-1)
[36]
          g.BReturnTuples[4] = [4]
[37]
          g.numberOfExits = 4
[38]
[39]
        return RepresentativeGrouping(g)
[40]
```

Figure 39:



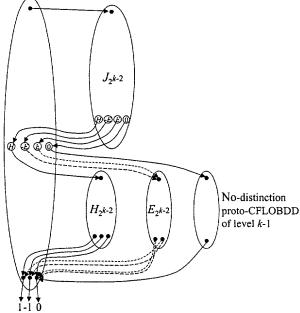
$$H_1 = \begin{array}{ccc} & 0 & 1 & y_0 \\ 1 & \hline 1 & -1 & \\ 1 & 1 & 1 \end{array}$$

(a) Level-1 CFLOBDD for the  $2 \times 2$  Boolean Haar Wavelet transform matrix  $H_1$ , under the interleaved variable ordering.



			0	0	1	1	$y_0$
			0	1	0	1	$y_1$
	0	0	1	-1	0	0	
$H_2 =$	0	1	1	1	-1	-1	
	1	0	0	0	1	-1	
	1	1	1	1	1	1	
	$x_0$	$x_1$					•

(b) Level-2 CFLOBDD for the  $4 \times 4$  Boolean Haar Wavelet transform matrix  $H_2$ , under the interleaved variable ordering.



(c) Schematic drawing showing how, under the interleaved variable ordering, the level-k CFLOBDD for the  $2^{2^{k-1}} \times 2^{2^{k-1}}$  Boolean Haar Wavelet transform matrix  $H_{2^{k-1}}$  is constructed from four level k-1 proto-CFLOBDDs.

Figure 40:

```
[1]
      CFLOBDD HaarCFLOBDD(int i) {
[2]
        if (i == 1) return RepresentativeCFLOBDD(HaarProtoCFLOBDD(1),[1,-1])
[3]
        else return RepresentativeCFLOBDD(HaarProtoCFLOBDD(i),[1,-1,0])
[4]
[5]
      InternalGrouping HaarProtoCFLOBDD(int i) {
[6]
        InternalGrouping g = new InternalGrouping(i)
[7]
        if (i == 1) {
[8]
          g.AConnection = RepresentativeForkGrouping
[9]
          g.AReturnTuple = [1,2]
[10]
          g.numberOfBConnections = 2
[11]
          g.BConnections[1] = RepresentativeForkGrouping
          g.BReturnTuples[1] = [1,2]
[12]
[13]
          g.BConnections[2] = RepresentativeDontCareGrouping
[14]
          g.BReturnTuples[2] = [1]
[15]
          g.numberOfExits = 2
[16]
[17]
        else if (i == 2) {
          g.AConnection = JProtoCFLOBDD(1)
[18]
[19]
          g.AReturnTuple = [1,2,3]
[20]
          g.numberOfBConnections = 3
[21]
          g.BConnections[1] = HaarProtoCFLOBDD(1)
[22]
          g.BReturnTuples[1] = [1,2]
          g.BConnections[2] = EProtoCFLOBDD(1)
[23]
[24]
          g.BReturnTuples[2] = [3,2]
[25]
          g.BConnections[3] = g.BConnections[2]
[26]
          g.BReturnTuples[3] = [3,1]
[27]
          g.numberOfExits = 3
[28]
[29]
        else {
[30]
          g.AConnection = JProtoCFLOBDD(i-1)
[31]
          g.AReturnTuple = [1,2,3,4]
[32]
          g.numberOfBConnections = 4
[33]
          g.BConnections[1] = HaarProtoCFLOBDD(i-1)
[34]
          g.BReturnTuples[1] = [1,2,3]
[35]
          g.BConnections[2] = EProtoCFLOBDD(i-1)
[36]
          g.BReturnTuples[2] = [3,2]
          g.BConnections[3] = g.BConnections[2]
[37]
[38]
          g.BReturnTuples[3] = [3,1]
          g.BConnections[4] = NoDistinctionProtoCFLOBDD(i-1)
[39]
[40]
          g.BReturnTuples[4] = [3]
[41]
          g.numberOfExits = 3
[42]
[43]
        return RepresentativeGrouping(g)
[44]
```

Figure 41:

```
[1]
      enum VisitState { FirstVisit, SecondVisit, ThirdVisit, Restart }
[2]
      class TraverseState {
        grouping: Grouping
[3]
[4]
        visitState: VisitState
[5]
        index: int // only relevant for when visitState == ThirdVisit
[6]
[7]
      ValueTuple UncompressCFLOBDD(CFLOBDD C) {
[8]
        ValueTuple ans = []
[9]
        Tuple of TraverseState S // Traversal stack; right end is top of stack
[10]
        Tuple of (Tuple of TraverseState) T // Stack of snapshots of S
[11]
        int exitVertexIndex
        T = [[new TraverseState(C.grouping,FirstVisit,_)]]
[12]
        while (T != []) {
[13]
[14]
          [T,S] = SplitOnLast(T) // S = last element of T; T = all of T but the last element
[15]
          while (S != []) {
            TraverseState [S,ts] = SplitOnLast(S) // ts = last element of S; S = all but last
[16]
[17]
            if (ts.grouping == RepresentativeForkGrouping) {
[18]
              if (ts.visitState == FirstVisit) { // follow the left branch
[19]
                T = T || (S || new TraverseState(ts.grouping, Restart,_)) // record snapshot
[20]
                exitVertexIndex = 1
[21]
[22]
              else { // ts.visitState == Restart; this time follow the right branch
[23]
                exitVertexIndex = 2
[24]
              }
[25]
[26]
            else if (ts.grouping == RepresentativeDontCareGrouping) {
[27]
              if (ts.visitState == FirstVisit) { // follow the left branch
                T = T || (S || new TraverseState(ts.grouping,Restart,_)) // record snapshot
[28]
[29]
                exitVertexIndex = 1
[30]
[31]
              else { // ts.visitState == Restart; this time follow the right branch
[32]
                exitVertexIndex = 1
[33]
              }
[34]
[35]
            else { // Must be a CFLOBDDInternalGrouping
[36]
              CFLOBDDInternalGrouping g = (CFLOBDDInternalGrouping)ts.grouping
[37]
              if (ts.visitState == FirstVisit) {
[38]
                S = S | | new TraverseState(g,SecondVisit,_)
[39]
                S = S | | new TraverseState(g.AConnection,FirstVisit,_)
[40]
              }
[41]
              else if (ts.visitState == SecondVisit) {
[42]
                int i = g.AReturnTuple[exitVertexIndex]
[43]
                S = S || new TraverseState(g,ThirdVisit,i)
[44]
                S = S | | new TraverseState(g.BConnection[i],FirstVisit,_)
[45]
[46]
              else { // ts.visitState == ThirdVisit
[47]
                exitVertexIndex = g.BReturnTuples[ts.index](exitVertexIndex)
[48]
[49]
            } // while (S != []) loop
          } // while (T != []) loop
[50]
          ans = ans || C.valueTuple[exitVertexIndex] // Finished processing one assignment
[51]
[52]
        }
[53]
       return ans
[54]
```